$$f(n,t,a,b) = \frac{t}{Beta(a,b)} \sum_{j=0}^{n-1} \sum_{k=0}^{j} \binom{j}{k} (1-t)^j Beta(a+k+1,b+j-k)$$

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